

Factorisation

(8.1)

1. $x^3 - 3x + 2$

$$= x^2(x-1) + x(x-1) - 2(x-1)$$

$$= (x-1)(x^2 + x - 2)$$

$$= (x-1)(x^2 + 2x - x - 2)$$

$$= (x-1) \{ x(x+2) - (x+2) \}$$

$$= (x-1)(x-1)(x+2) \quad \underline{\text{Ans.}}$$

2. $x^3 + 2x + 3$

$$= x^2(x+1) - x(x+1) + 3(x+1)$$

$$= (x+1)(x^2 - x + 3) \quad \underline{\text{Ans.}}$$

~~$(x+1)$~~

3. $a^3 - 12a - 16$

$$= a^2(a+2) - 2a(a+2) - 8(a+2)$$

$$= (a+2)(a^2 - 2a - 8)$$

$$= (a+2) \{ a^2 - 4a + 2a - 8 \}$$

$$= (a+2) \{ a(a-4) + 2(a-4) \}$$

$$= (a+2)(a+2)(a-4) \quad \underline{\text{Ans.}}$$

$$(4) \quad x^3 - 6x + 4$$

$$= x^2(x-2) + 2x(x-2) - 2(x-2)$$

$$= (x-2)(x^2 + 2x - 2)$$

$$(5) \quad x^3 - 19x - 30$$

$$= -x^2(x+2) + 2x(x+2) - 15(x+2)$$

$$= x^2(x+2) - 2x(x+2) - 15(x+2)$$

$$= (x+2)(x^2 - 2x - 15)$$

$$= (x+2)(x^2 - 5x + 3x - 15)$$

$$= (x+2)\{x(x-5) + 3(x-5)\}$$

$$= (x+2)(x-5)(x+3)$$

$$(6) \quad 4a^3 - 9a^2 + 3a + 2$$

$$= 4a^2(a-1) - 5a(a-1) - 2(a-1)$$

$$= (a-1)(4a^2 - 5a - 2)$$

$$= (a-1)(4a^2 - 5a - 2)$$

$$(7) \quad x^3 - 9x^2 + 23x - 15$$

$$= x^2(x-1) - 8x(x-1) + 15(x-1)$$

$$= (x-1)(x^2 - 8x + 15)$$

$$= (x-1)(x^2 - 5x - 3x + 15)$$

$$= (x-1)(x-5)(x-3)$$

$$\begin{aligned}
 8. \quad & 5a^3 + 11a^2 + 4a - 2 \\
 & = 5a^2(a+1) + 6a(a+1) - 2(a+1) \\
 & = (a+1)(5a^2 + 6a - 2)
 \end{aligned}$$

$$\begin{aligned}
 9. \quad & 2x^3 - x^2 + 9x + 5 \\
 & = x^2(2x+1) - x(2x+1) + 5(2x+1) \\
 & = (2x+1)(x^2 - x + 5)
 \end{aligned}$$

$$\begin{aligned}
 10. \quad & 2y^3 - 5y^2 - 19y + 42 \\
 & = 2y^2(y-2) - 7y(y-2) + 21(y-2) \\
 & = (y-2)(2y^2 - 7y + 21) \\
 & = (y-2) \left\{ 2y^2 - 7y + 6y - 21 \right\} \\
 & = (y-2) \left\{ y(2y-7) + 3(2y-7) \right\} \\
 & = (y-2)(2y-7)(y+3)
 \end{aligned}$$